

## The Crystal Structure of 2,4,6-Trimethylbenzoic Acid

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Crystals of 2,4,6-trimethylbenzoic acid are monoclinic with space group  $C2/c$  and have eight molecules in the unit cell. The structure has been determined by Patterson and trial and error methods and refined by Fourier and three-dimensional differential syntheses. The benzene ring is planar, and C-C distances average 1.391 Å; the carboxyl group however is twisted  $48^\circ 29'$  from this plane. All intermolecular contacts correspond to normal van der Waals interactions.

### Introduction

The study of the structure of 2,4,6-trimethylbenzoic acid has been carried out in an attempt to determine the characteristics of the interactions between the methyl groups and the carboxyl group in this molecule.

Similar studies on this kind of interaction in other organic molecules have been reported by several authors: Ferguson & Sim (1961, 1962) on *o*-bromobenzoic acid, and *o*-chlorobenzoic acid, and Brown & Marsh (1963) on 2-amino-3-methylbenzoic acid, found similar values for the angle between the plane of the benzene ring and the plane of the carboxyl group. Anca, Martínez-Carrera & García-Blanco (1967) found a much larger tilt in 2,6-dimethylbenzoic acid, which corresponds to a compound bisubstituted in the *ortho* position relative to the carboxyl group. Lai & Marsh (1967) found a much smaller angle in *p*-aminobenzoic acid. The present study shows that in this respect 2,4,6-trimethylbenzoic acid possesses the properties of both *ortho* and *para* substituted compounds.

### Experimental

Crystals of 2,4,6-trimethylbenzoic acid were readily grown from solution in ethanol. A prismatic needle of length 0.30 mm and 0.10 × 0.15 mm section was used for collection about the *b* axis, and a tabular crystal of 0.20 × 0.25 mm for collection about the *a* axis. The crystal data, obtained from measurements on zero level Weissenberg photographs about the two axes, are:

$$\begin{aligned} a &= 15.21 \pm 0.01 \text{ \AA} \\ b &= 7.02 \pm 0.01 \\ c &= 17.54 \pm 0.01 \\ \beta &= 90^\circ 43' \\ D_m &= 1.16 \text{ g.cm}^{-3}, D_x = 1.156 \text{ g.cm}^{-3}, Z = 8 \end{aligned}$$

Systematic absences are:  $hkl$  with  $h+k \neq 2n$ ,  $h0l$  with  $l \neq 2n$ , corresponding to two possible space groups,  $C2/c$  and  $Cc$ ; the first space group was confirmed by solution of the structure.

X-ray intensities were collected from multiple-film equi-inclination Weissenberg photographs with Cu  $K\alpha$  radiation. Eight layers recorded by rotation about **b** and five layers recorded by rotation about **a** were measured photometrically. Copper radiation allows a maximum of 1217 unique reflexions, representing 66% of the possible observable number. Unobserved reflexions were included by taking one half of the minimum observable intensity.

Data from the two axes were corrected for Lorentz and polarization factors and those of the non-zero layers for the spot extension factor also. No correction for absorption was made.

The data were reduced to structure amplitudes in the usual way, and placed on the same relative scale by means of a comparison of common reflexions on different films. Observed and calculated structure factors are given in Table 1.

### Determination of the structure

Because the molecule was presumed to be planar and centrosymmetric, as is the case in other analogous acids, and because there are just eight molecules in the unit cell, it seemed likely that the space group was the centrosymmetric one,  $C2/c$ , rather than  $Cc$ . Accordingly the molecules were centred either at (000) or at  $(\frac{1}{4}\frac{1}{4}0)$ , these being the two unique centres of symmetry in  $C2/c$ .

The positions and orientations of the molecules were determined by computing the structure factors of seven  $h00$ , four  $0k0$  and eleven  $00l$  reflexions as a function of a rotation matrix, and also by interpretation of a sharpened three-dimensional Patterson function.

The  $F(hkl)^2$  were multiplied by the factor

$$(1/f) \exp(2B \sin^2 \theta / \lambda^2) (2 \sin \theta / \lambda)^4 \exp[-(4.4 \sin \theta / \lambda)^2]$$

(Donohue & Trueblood, 1952; Brown & Marsh, 1963).

In this way a set of  $x, y, z$  coordinates for the heavy atoms was obtained. Structure factors were calculated

Table 1. *Observed and calculated structure factors*

Unobserved reflexions are marked with an asterisk

| H   | K | L | FOBS  | FCAL  | H  | K | L  | FOBS | FCAL | H | K | L | FOBS | FCAL | H | K | L | FOBS | FCAL | H | K | L | FOBS | FCAL |
|-----|---|---|-------|-------|----|---|----|------|------|---|---|---|------|------|---|---|---|------|------|---|---|---|------|------|
| 2   |   |   | 78.4  | 78.4  | -1 | 3 | 11 | 25.7 | 26.2 | 2 | 2 | 1 | 71.1 | 71.2 | 5 | 1 | 4 | 31.7 | 32.4 | 4 | 4 |   | 2.4  | 2.4  |
| 4   |   |   | 114.1 | 114.1 | -1 | 3 | 12 | 25.0 | 25.0 | 2 | 2 | 1 | 14.1 | 14.2 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 40.6 | 40.6 |
| 6   |   |   | 79.8  | 79.8  | -1 | 3 | 13 | 11.4 | 11.4 | 2 | 2 | 1 | 44.4 | 44.4 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 18.7 | 18.7 |
| 8   |   |   | 111.0 | 111.0 | -1 | 3 | 14 | 16.4 | 16.4 | 2 | 2 | 1 | 25.9 | 26.0 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 10.8 | 10.8 |
| 10  |   |   | 71.0  | 71.0  | -1 | 3 | 15 | 33.7 | 34.1 | 2 | 2 | 1 | 77.6 | 77.6 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 13.0 | 13.0 |
| 12  |   |   | 74.8  | 74.8  | -1 | 3 | 16 | 4.4  | 4.4  | 2 | 2 | 1 | 9.1  | 9.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 13.4 | 13.4 |
| 14  |   |   | 111.7 | 111.7 | -1 | 3 | 17 | 10.4 | 10.4 | 2 | 2 | 1 | 21.5 | 21.5 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 13.4 | 13.4 |
| 16  |   |   | 4.0   | 4.0   | -1 | 3 | 18 | 10.8 | 11.1 | 2 | 2 | 1 | 71.5 | 71.5 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 20.0 | 20.0 |
| 18  |   |   | 62.7  | 62.7  | -1 | 3 | 19 | 8.0  | 8.0  | 2 | 2 | 1 | 42.0 | 42.0 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 7.9  | 7.9  |
| 20  |   |   | 24.8  | 24.8  | -1 | 3 | 20 | 20.8 | 20.8 | 2 | 2 | 1 | 4.0  | 4.0  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 8.0  | 8.0  |
| 22  |   |   | 42.7  | 42.7  | -1 | 3 | 21 | 11.7 | 11.7 | 2 | 2 | 1 | 11.4 | 11.4 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 1.01 | 1.01 |
| 24  |   |   | 84.1  | 84.1  | -1 | 3 | 22 | 70.7 | 70.7 | 2 | 2 | 1 | 17.1 | 17.1 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.21 | 4.21 |
| 26  |   |   | 25.0  | 25.0  | -1 | 3 | 23 | 44.0 | 44.0 | 2 | 2 | 1 | 15.0 | 15.0 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 2.0  | 2.0  |
| 28  |   |   | 46.9  | 46.9  | -1 | 3 | 24 | 39.6 | 39.6 | 2 | 2 | 1 | 11.4 | 11.4 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 2.0  | 2.0  |
| 30  |   |   | 10.2  | 10.2  | -1 | 3 | 25 | 19.6 | 19.6 | 2 | 2 | 1 | 26.8 | 26.8 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 2.0  | 2.0  |
| 32  |   |   | 11.1  | 11.1  | -1 | 3 | 26 | 10.1 | 10.1 | 2 | 2 | 1 | 15.6 | 15.6 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 2.0  | 2.0  |
| 34  |   |   | 11.1  | 11.1  | -1 | 3 | 27 | 48.4 | 48.1 | 2 | 2 | 1 | 19.6 | 19.6 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 0.1  | 0.1  |
| 36  |   |   | 11.1  | 11.1  | -1 | 3 | 28 | 78.4 | 78.4 | 2 | 2 | 1 | 21.7 | 21.7 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.0  | 4.0  |
| 38  |   |   | 72.8  | 72.8  | -1 | 3 | 29 | 10.4 | 10.4 | 2 | 2 | 1 | 21.0 | 21.0 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 1.01 | 1.01 |
| 40  |   |   | 68.0  | 68.0  | -1 | 3 | 30 | 10.9 | 10.9 | 2 | 2 | 1 | 16.4 | 16.4 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 2.0  | 2.0  |
| 42  |   |   | 25.7  | 25.7  | -1 | 3 | 31 | 17.1 | 17.1 | 2 | 2 | 1 | 10.7 | 10.7 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 2.0  | 2.0  |
| 44  |   |   | 40.4  | 40.4  | -1 | 3 | 32 | 28.7 | 28.7 | 2 | 2 | 1 | 2.7  | 2.7  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 2.1  | 2.1  |
| 46  |   |   | 27.1  | 27.1  | -1 | 3 | 33 | 4.0  | 4.0  | 2 | 2 | 1 | 1.4  | 1.4  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 3.0  | 3.0  |
| 48  |   |   | 6.2   | 6.2   | -1 | 3 | 34 | 24.8 | 24.8 | 2 | 2 | 1 | 10.8 | 10.8 | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.0  | 4.0  |
| 50  |   |   | 19.2  | 19.2  | -1 | 3 | 35 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 52  |   |   | 19.2  | 19.2  | -1 | 3 | 36 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 54  |   |   | 19.2  | 19.2  | -1 | 3 | 37 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 56  |   |   | 19.2  | 19.2  | -1 | 3 | 38 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 58  |   |   | 19.2  | 19.2  | -1 | 3 | 39 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 60  |   |   | 19.2  | 19.2  | -1 | 3 | 40 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 62  |   |   | 19.2  | 19.2  | -1 | 3 | 41 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 64  |   |   | 19.2  | 19.2  | -1 | 3 | 42 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 66  |   |   | 19.2  | 19.2  | -1 | 3 | 43 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 68  |   |   | 19.2  | 19.2  | -1 | 3 | 44 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 70  |   |   | 19.2  | 19.2  | -1 | 3 | 45 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 72  |   |   | 19.2  | 19.2  | -1 | 3 | 46 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 74  |   |   | 19.2  | 19.2  | -1 | 3 | 47 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 76  |   |   | 19.2  | 19.2  | -1 | 3 | 48 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 78  |   |   | 19.2  | 19.2  | -1 | 3 | 49 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 80  |   |   | 19.2  | 19.2  | -1 | 3 | 50 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 82  |   |   | 19.2  | 19.2  | -1 | 3 | 51 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 84  |   |   | 19.2  | 19.2  | -1 | 3 | 52 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 86  |   |   | 19.2  | 19.2  | -1 | 3 | 53 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 88  |   |   | 19.2  | 19.2  | -1 | 3 | 54 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 90  |   |   | 19.2  | 19.2  | -1 | 3 | 55 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 92  |   |   | 19.2  | 19.2  | -1 | 3 | 56 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 94  |   |   | 19.2  | 19.2  | -1 | 3 | 57 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 96  |   |   | 19.2  | 19.2  | -1 | 3 | 58 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 98  |   |   | 19.2  | 19.2  | -1 | 3 | 59 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 100 |   |   | 19.2  | 19.2  | -1 | 3 | 60 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 102 |   |   | 19.2  | 19.2  | -1 | 3 | 61 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 104 |   |   | 19.2  | 19.2  | -1 | 3 | 62 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 106 |   |   | 19.2  | 19.2  | -1 | 3 | 63 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 108 |   |   | 19.2  | 19.2  | -1 | 3 | 64 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 110 |   |   | 19.2  | 19.2  | -1 | 3 | 65 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 112 |   |   | 19.2  | 19.2  | -1 | 3 | 66 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 114 |   |   | 19.2  | 19.2  | -1 | 3 | 67 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 116 |   |   | 19.2  | 19.2  | -1 | 3 | 68 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 118 |   |   | 19.2  | 19.2  | -1 | 3 | 69 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 120 |   |   | 19.2  | 19.2  | -1 | 3 | 70 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 122 |   |   | 19.2  | 19.2  | -1 | 3 | 71 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 124 |   |   | 19.2  | 19.2  | -1 | 3 | 72 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 126 |   |   | 19.2  | 19.2  | -1 | 3 | 73 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 128 |   |   | 19.2  | 19.2  | -1 | 3 | 74 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 130 |   |   | 19.2  | 19.2  | -1 | 3 | 75 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 132 |   |   | 19.2  | 19.2  | -1 | 3 | 76 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 134 |   |   | 19.2  | 19.2  | -1 | 3 | 77 | 10.2 | 10.2 | 2 | 2 | 1 | 2.1  | 2.1  | 5 | 1 | 4 | 23.2 | 23.4 | 4 | 4 |   | 4.1  | 4.1  |
| 136 |   |   | 19.2  | 19.2  | -1 | 3 | 78 | 10.2 | 10.2 | 2 | 2 |   |      |      |   |   |   |      |      |   |   |   |      |      |

Table 1 (cont.)

| H  | K | L   | FOBS | FCAL  | H  | K | L  | FOBS | FCAL | H  | K | L   | FOBS | FCAL | H | K | L   | FOBS | FCAL |
|----|---|-----|------|-------|----|---|----|------|------|----|---|-----|------|------|---|---|-----|------|------|
| -8 | 1 | 21  | 1.0  | 4.11E | 8  | 7 | 8  | 1.2  | 17.7 | -8 | 8 | 2   | 1.2  | 16.2 | 7 | 7 | 1   | 8.1  | 6.7  |
| -8 | 1 | 20  | 2.4  | 1.4E  | 8  | 7 | 9  | 8.2  | 2.7E | -8 | 8 | 2   | 1.2  | 16.2 | 7 | 7 | 1   | 7.1  | 5.7  |
| -8 | 1 | 19  | 4.2  | 6.2E  | 8  | 7 | 10 | 2.7  | 2.1  | -8 | 8 | 4   | 1.2  | 17.2 | 7 | 7 | 2   | 4.4  | 3.6  |
| -8 | 1 | 18  | 6.2  | 8.2E  | 8  | 7 | 11 | 2.2  | 2.2  | -8 | 8 | 6   | 1.2  | 18.2 | 7 | 7 | 4   | 4.2  | 4.0  |
| -8 | 1 | 17  | 8.2  | 8.2E  | 8  | 7 | 12 | 1.2  | 2.2  | -8 | 8 | 8   | 1.2  | 19.2 | 7 | 7 | 6   | 4.2  | 4.0  |
| -8 | 1 | 16  | 8.1  | 2.1E  | -8 | 7 | 13 | 1.2  | 2.2  | -8 | 8 | 10  | 1.2  | 20.2 | 7 | 7 | 8   | 4.2  | 4.0  |
| -8 | 1 | 15  | 10.2 | 9.1E  | -8 | 7 | 14 | 0.2  | 2.2  | -8 | 8 | 12  | 1.2  | 21.2 | 7 | 7 | 10  | 4.2  | 4.0  |
| -8 | 1 | 14  | 11.2 | 11.7E | -8 | 7 | 15 | 0.2  | 2.2  | -8 | 8 | 14  | 1.2  | 22.2 | 7 | 7 | 12  | 4.2  | 4.0  |
| -8 | 1 | 13  | 10.2 | 1.2E  | -8 | 7 | 16 | 0.2  | 2.2  | -8 | 8 | 16  | 1.2  | 23.2 | 7 | 7 | 14  | 4.2  | 4.0  |
| -8 | 1 | 12  | 8.2  | 1.2E  | -8 | 7 | 17 | 0.2  | 2.2  | -8 | 8 | 18  | 1.2  | 24.2 | 7 | 7 | 16  | 4.2  | 4.0  |
| -8 | 1 | 11  | 6.2  | 1.2E  | -8 | 7 | 18 | 0.2  | 2.2  | -8 | 8 | 20  | 1.2  | 25.2 | 7 | 7 | 18  | 4.2  | 4.0  |
| -8 | 1 | 10  | 11.2 | 11.7E | -8 | 7 | 19 | 1.2  | 1.2  | -8 | 8 | 22  | 1.2  | 26.2 | 7 | 7 | 20  | 4.2  | 4.0  |
| -8 | 1 | 9   | 13.2 | 13.2E | -8 | 7 | 20 | 1.2  | 1.2  | -8 | 8 | 24  | 1.2  | 27.2 | 7 | 7 | 22  | 4.2  | 4.0  |
| -8 | 1 | 8   | 9.2  | 9.2E  | -8 | 7 | 21 | 1.2  | 1.2  | -8 | 8 | 26  | 1.2  | 28.2 | 7 | 7 | 24  | 4.2  | 4.0  |
| -8 | 1 | 7   | 8.2  | 9.2E  | -8 | 7 | 22 | 1.2  | 1.2  | -8 | 8 | 28  | 1.2  | 29.2 | 7 | 7 | 26  | 4.2  | 4.0  |
| -8 | 1 | 6   | 7.2  | 8.2E  | -8 | 7 | 23 | 1.2  | 1.2  | -8 | 8 | 30  | 1.2  | 30.2 | 7 | 7 | 28  | 4.2  | 4.0  |
| -8 | 1 | 5   | 6.2  | 7.2E  | -8 | 7 | 24 | 1.2  | 1.2  | -8 | 8 | 32  | 1.2  | 31.2 | 7 | 7 | 30  | 4.2  | 4.0  |
| -8 | 1 | 4   | 5.2  | 6.2E  | -8 | 7 | 25 | 1.2  | 1.2  | -8 | 8 | 34  | 1.2  | 32.2 | 7 | 7 | 32  | 4.2  | 4.0  |
| -8 | 1 | 3   | 4.2  | 5.2E  | -8 | 7 | 26 | 1.2  | 1.2  | -8 | 8 | 36  | 1.2  | 33.2 | 7 | 7 | 34  | 4.2  | 4.0  |
| -8 | 1 | 2   | 3.2  | 4.2E  | -8 | 7 | 27 | 1.2  | 1.2  | -8 | 8 | 38  | 1.2  | 34.2 | 7 | 7 | 36  | 4.2  | 4.0  |
| -8 | 1 | 1   | 2.2  | 3.2E  | -8 | 7 | 28 | 1.2  | 1.2  | -8 | 8 | 40  | 1.2  | 35.2 | 7 | 7 | 38  | 4.2  | 4.0  |
| -8 | 1 | 0   | 1.2  | 2.2E  | -8 | 7 | 29 | 1.2  | 1.2  | -8 | 8 | 42  | 1.2  | 36.2 | 7 | 7 | 40  | 4.2  | 4.0  |
| -8 | 1 | -1  | 0.2  | 1.2E  | -8 | 7 | 30 | 1.2  | 1.2  | -8 | 8 | 44  | 1.2  | 37.2 | 7 | 7 | 42  | 4.2  | 4.0  |
| -8 | 1 | -2  | -0.2 | 0.2E  | -8 | 7 | 31 | 1.2  | 1.2  | -8 | 8 | 46  | 1.2  | 38.2 | 7 | 7 | 44  | 4.2  | 4.0  |
| -8 | 1 | -3  | -0.2 | -0.2E | -8 | 7 | 32 | 1.2  | 1.2  | -8 | 8 | 48  | 1.2  | 39.2 | 7 | 7 | 46  | 4.2  | 4.0  |
| -8 | 1 | -4  | -0.2 | -0.2E | -8 | 7 | 33 | 1.2  | 1.2  | -8 | 8 | 50  | 1.2  | 40.2 | 7 | 7 | 48  | 4.2  | 4.0  |
| -8 | 1 | -5  | -0.2 | -0.2E | -8 | 7 | 34 | 1.2  | 1.2  | -8 | 8 | 52  | 1.2  | 41.2 | 7 | 7 | 50  | 4.2  | 4.0  |
| -8 | 1 | -6  | -0.2 | -0.2E | -8 | 7 | 35 | 1.2  | 1.2  | -8 | 8 | 54  | 1.2  | 42.2 | 7 | 7 | 52  | 4.2  | 4.0  |
| -8 | 1 | -7  | -0.2 | -0.2E | -8 | 7 | 36 | 1.2  | 1.2  | -8 | 8 | 56  | 1.2  | 43.2 | 7 | 7 | 54  | 4.2  | 4.0  |
| -8 | 1 | -8  | -0.2 | -0.2E | -8 | 7 | 37 | 1.2  | 1.2  | -8 | 8 | 58  | 1.2  | 44.2 | 7 | 7 | 56  | 4.2  | 4.0  |
| -8 | 1 | -9  | -0.2 | -0.2E | -8 | 7 | 38 | 1.2  | 1.2  | -8 | 8 | 60  | 1.2  | 45.2 | 7 | 7 | 58  | 4.2  | 4.0  |
| -8 | 1 | -10 | -0.2 | -0.2E | -8 | 7 | 39 | 1.2  | 1.2  | -8 | 8 | 62  | 1.2  | 46.2 | 7 | 7 | 60  | 4.2  | 4.0  |
| -8 | 1 | -11 | -0.2 | -0.2E | -8 | 7 | 40 | 1.2  | 1.2  | -8 | 8 | 64  | 1.2  | 47.2 | 7 | 7 | 62  | 4.2  | 4.0  |
| -8 | 1 | -12 | -0.2 | -0.2E | -8 | 7 | 41 | 1.2  | 1.2  | -8 | 8 | 66  | 1.2  | 48.2 | 7 | 7 | 64  | 4.2  | 4.0  |
| -8 | 1 | -13 | -0.2 | -0.2E | -8 | 7 | 42 | 1.2  | 1.2  | -8 | 8 | 68  | 1.2  | 49.2 | 7 | 7 | 66  | 4.2  | 4.0  |
| -8 | 1 | -14 | -0.2 | -0.2E | -8 | 7 | 43 | 1.2  | 1.2  | -8 | 8 | 70  | 1.2  | 50.2 | 7 | 7 | 68  | 4.2  | 4.0  |
| -8 | 1 | -15 | -0.2 | -0.2E | -8 | 7 | 44 | 1.2  | 1.2  | -8 | 8 | 72  | 1.2  | 51.2 | 7 | 7 | 70  | 4.2  | 4.0  |
| -8 | 1 | -16 | -0.2 | -0.2E | -8 | 7 | 45 | 1.2  | 1.2  | -8 | 8 | 74  | 1.2  | 52.2 | 7 | 7 | 72  | 4.2  | 4.0  |
| -8 | 1 | -17 | -0.2 | -0.2E | -8 | 7 | 46 | 1.2  | 1.2  | -8 | 8 | 76  | 1.2  | 53.2 | 7 | 7 | 74  | 4.2  | 4.0  |
| -8 | 1 | -18 | -0.2 | -0.2E | -8 | 7 | 47 | 1.2  | 1.2  | -8 | 8 | 78  | 1.2  | 54.2 | 7 | 7 | 76  | 4.2  | 4.0  |
| -8 | 1 | -19 | -0.2 | -0.2E | -8 | 7 | 48 | 1.2  | 1.2  | -8 | 8 | 80  | 1.2  | 55.2 | 7 | 7 | 78  | 4.2  | 4.0  |
| -8 | 1 | -20 | -0.2 | -0.2E | -8 | 7 | 49 | 1.2  | 1.2  | -8 | 8 | 82  | 1.2  | 56.2 | 7 | 7 | 80  | 4.2  | 4.0  |
| -8 | 1 | -21 | -0.2 | -0.2E | -8 | 7 | 50 | 1.2  | 1.2  | -8 | 8 | 84  | 1.2  | 57.2 | 7 | 7 | 82  | 4.2  | 4.0  |
| -8 | 1 | -22 | -0.2 | -0.2E | -8 | 7 | 51 | 1.2  | 1.2  | -8 | 8 | 86  | 1.2  | 58.2 | 7 | 7 | 84  | 4.2  | 4.0  |
| -8 | 1 | -23 | -0.2 | -0.2E | -8 | 7 | 52 | 1.2  | 1.2  | -8 | 8 | 88  | 1.2  | 59.2 | 7 | 7 | 86  | 4.2  | 4.0  |
| -8 | 1 | -24 | -0.2 | -0.2E | -8 | 7 | 53 | 1.2  | 1.2  | -8 | 8 | 90  | 1.2  | 60.2 | 7 | 7 | 88  | 4.2  | 4.0  |
| -8 | 1 | -25 | -0.2 | -0.2E | -8 | 7 | 54 | 1.2  | 1.2  | -8 | 8 | 92  | 1.2  | 61.2 | 7 | 7 | 90  | 4.2  | 4.0  |
| -8 | 1 | -26 | -0.2 | -0.2E | -8 | 7 | 55 | 1.2  | 1.2  | -8 | 8 | 94  | 1.2  | 62.2 | 7 | 7 | 92  | 4.2  | 4.0  |
| -8 | 1 | -27 | -0.2 | -0.2E | -8 | 7 | 56 | 1.2  | 1.2  | -8 | 8 | 96  | 1.2  | 63.2 | 7 | 7 | 94  | 4.2  | 4.0  |
| -8 | 1 | -28 | -0.2 | -0.2E | -8 | 7 | 57 | 1.2  | 1.2  | -8 | 8 | 98  | 1.2  | 64.2 | 7 | 7 | 96  | 4.2  | 4.0  |
| -8 | 1 | -29 | -0.2 | -0.2E | -8 | 7 | 58 | 1.2  | 1.2  | -8 | 8 | 100 | 1.2  | 65.2 | 7 | 7 | 98  | 4.2  | 4.0  |
| -8 | 1 | -30 | -0.2 | -0.2E | -8 | 7 | 59 | 1.2  | 1.2  | -8 | 8 | 102 | 1.2  | 66.2 | 7 | 7 | 100 | 4.2  | 4.0  |
| -8 | 1 | -31 | -0.2 | -0.2E | -8 | 7 | 60 | 1.2  | 1.2  | -8 | 8 | 104 | 1.2  | 67.2 | 7 | 7 | 102 | 4.2  | 4.0  |
| -8 | 1 | -32 | -0.2 | -0.2E | -8 | 7 | 61 | 1.2  | 1.2  | -8 | 8 | 106 | 1.2  | 68.2 | 7 | 7 | 104 | 4.2  | 4.0  |
| -8 | 1 | -33 | -0.2 | -0.2E | -8 | 7 | 62 | 1.2  | 1.2  | -8 | 8 | 108 | 1.2  | 69.2 | 7 | 7 | 106 | 4.2  | 4.0  |
| -8 | 1 | -34 | -0.2 | -0.2E | -8 | 7 | 63 | 1.2  | 1.2  | -8 | 8 | 110 | 1.2  | 70.2 | 7 | 7 | 108 | 4.2  | 4.0  |
| -8 | 1 | -35 | -0.2 | -0.2E | -8 | 7 | 64 | 1.2  | 1.2  | -8 | 8 | 112 | 1.2  | 71.2 | 7 | 7 | 110 | 4.2  | 4.0  |
| -8 | 1 | -36 | -0.2 | -0.2E | -8 | 7 | 65 | 1.2  | 1.2  | -8 | 8 | 114 | 1.2  | 72.2 | 7 | 7 | 112 | 4.2  | 4.0  |
| -8 | 1 | -37 | -0.2 | -0.2E | -8 | 7 | 66 | 1.2  | 1.2  | -8 | 8 | 116 | 1.2  | 73.2 | 7 | 7 | 114 | 4.2  | 4.0  |
| -8 | 1 | -38 | -0.2 | -0.2E | -8 | 7 | 67 | 1.2  | 1.2  | -8 | 8 | 118 | 1.2  | 74.2 | 7 | 7 | 116 | 4.2  | 4.0  |
| -8 | 1 | -39 | -0.2 | -0.2E | -8 | 7 | 68 | 1.2  | 1.2  | -8 | 8 | 120 | 1.2  | 75.2 | 7 | 7 | 118 | 4.2  | 4.0  |
| -8 | 1 | -40 | -0.2 | -0.2E | -8 | 7 | 69 | 1.2  | 1.2  | -8 | 8 | 122 | 1.2  | 76.2 | 7 | 7 | 120 | 4.2  | 4.0  |
| -8 | 1 | -41 | -0.2 | -0.2E | -8 | 7 | 70 | 1.2  | 1.2  | -8 | 8 | 124 | 1.2  | 77.2 | 7 | 7 | 122 | 4.2  | 4.0  |
| -8 | 1 | -42 | -0.2 | -0.2E | -8 | 7 | 71 | 1.2  | 1.2  | -8 | 8 | 126 | 1.2  | 78.2 | 7 | 7 | 124 | 4.2  | 4.0  |
| -8 | 1 | -43 | -0.2 | -0.2E | -8 | 7 | 72 | 1.2  | 1.2  | -8 | 8 | 128 | 1.2  | 79.2 | 7 | 7 | 126 | 4.2  | 4.0  |
| -8 | 1 | -44 | -0.2 | -0.2E | -8 | 7 | 73 | 1.2  | 1.2  | -8 | 8 | 130 | 1.2  | 80.2 | 7 | 7 | 128 | 4.2  | 4.0  |
| -8 | 1 | -45 | -0.2 | -0.2E | -8 | 7 | 74 | 1.2  | 1.2  | -8 | 8 | 132 | 1.2  | 81.2 | 7 | 7 | 130 | 4.2  | 4.0  |
| -8 | 1 | -46 | -0.2 | -0.2E | -8 | 7 | 75 | 1.2  | 1.2  | -8 | 8 | 134 | 1.2  | 82.2 | 7 | 7 | 132 | 4.2  | 4.0  |
| -8 | 1 | -47 | -0.2 | -0.2E | -8 | 7 | 76 | 1.2  | 1.2  | -8 | 8 | 136 | 1.2  | 83.2 | 7 | 7 | 134 | 4.2  | 4.0  |
| -8 | 1 | -48 | -0.2 | -0.2E | -8 | 7 | 77 | 1.2  | 1.2  | -8 | 8 | 138 | 1.2  | 84.2 | 7 | 7 | 136 | 4.2  | 4.0  |
| -8 | 1 | -49 | -0.2 | -0.2E | -8 | 7 | 78 | 1.2  | 1.2  | -8 | 8 | 140 | 1.2  | 85.2 | 7 | 7 | 138 | 4.2  | 4.0  |
| -8 | 1 | -50 | -0.2 | -0.2E | -8 | 7 | 79 | 1.2  | 1.2  | -8 | 8 | 142 | 1.2  | 86.2 | 7 | 7 | 140 | 4.2  | 4.0  |
| -8 | 1 | -51 | -0.2 | -0.2E | -8 | 7 | 80 | 1.2  | 1.2  | -8 | 8 | 144 | 1.2  | 87.2 | 7 | 7 | 142 | 4.2  | 4.0  |
| -8 | 1 | -52 | -0.2 | -0.2E | -8 | 7 | 81 | 1.2  | 1.2  | -8 | 8 | 146 | 1.2  | 88.2 | 7 | 7 | 144 | 4.2  | 4.0  |
| -8 | 1 | -53 | -0.2 | -0.2E | -8 | 7 | 82 | 1.2  | 1.2  | -8 | 8 | 148 | 1.2  | 89.2 | 7 | 7 | 146 | 4.2  | 4.0  |
| -8 | 1 | -54 | -0.2 | -0.2E | -8 | 7 | 83 | 1.2  | 1.2  | -8 | 8 | 150 | 1.2  | 90.2 | 7 | 7 | 148 | 4.2  | 4.0  |
| -8 | 1 | -55 | -0.2 | -0.2E | -8 | 7 | 84 | 1.2  | 1.2  | -8 | 8 | 152 | 1.2  | 91.2 | 7 | 7 | 150 | 4.2  | 4.0  |
| -8 | 1 | -56 | -0.2 | -0.2E | -8 | 7 | 85 | 1.2  | 1.2  | -8 | 8 | 154 | 1.2  | 92.2 | 7 | 7 | 152 | 4.2  | 4.0  |
| -8 | 1 | -57 | -0.2 | -0.2E | -8 | 7 | 86 | 1.2  | 1.2  | -8 | 8 | 156 | 1.2  | 93.2 | 7 | 7 | 154 | 4.2  | 4.0  |
| -8 | 1 | -58 | -0.2 | -0.2E | -8 | 7 | 87 | 1.2  | 1.2  | -8 | 8 | 158 | 1.2  | 94.2 | 7 | 7 | 156 | 4.2  | 4.0  |
| -8 | 1 | -59 | -0.2 | -0.2E | -8 | 7 | 88 | 1.2  | 1.2  | -8 | 8 | 160 | 1.2  | 95.2 | 7 | 7 | 158 | 4.2  | 4.0  |
| -8 | 1 | -60 | -0.2 | -0.2E | -8 | 7 | 89 | 1.2  | 1.2  | -8 | 8 | 162 | 1.2  | 96.2 | 7 | 7 | 160 | 4.2  |      |

Table 1 (cont.)

| H   | K | L  | FQBS | FCAL | H   | K | L  | FQBS | FCAL | H   | K | L  | FQBS | FCAL | H  | K | L  | FQBS | FCAL | H  | K | L  | FQBS | FCAL |
|-----|---|----|------|------|-----|---|----|------|------|-----|---|----|------|------|----|---|----|------|------|----|---|----|------|------|
| -11 | 1 | 14 | 10.7 | 11.7 | -12 | 2 | 13 | 2.0  | 2.8  | 13  | 1 | 15 | 6.0  | 6.0  | 14 | 4 | 1  | 7.1  | 7.1  | 14 | 2 | 1  | 9.0  | 9.0  |
| -11 | 1 | 14 | 6.0  | 6.6  | -12 | 2 | 13 | 1.2  | 1.2  | -13 | 1 | 14 | 2.8  | 2.8  | 14 | 4 | 2  | 7.1  | 7.1  | 14 | 2 | 2  | 9.0  | 9.0  |
| -11 | 1 | 14 | 5.7  | 6.7  | -12 | 2 | 13 | 5.2  | 5.2  | -13 | 1 | 14 | 3.8  | 3.8  | 14 | 4 | 3  | 7.1  | 7.1  | 14 | 2 | 3  | 9.0  | 9.0  |
| -11 | 1 | 14 | 5.8  | 6.8  | -12 | 2 | 13 | 5.4  | 5.4  | -13 | 1 | 14 | 3.9  | 3.9  | 14 | 4 | 4  | 7.1  | 7.1  | 14 | 2 | 4  | 9.0  | 9.0  |
| -11 | 1 | 14 | 5.9  | 6.9  | -12 | 2 | 13 | 5.6  | 5.6  | -13 | 1 | 14 | 4.0  | 4.0  | 14 | 4 | 5  | 7.1  | 7.1  | 14 | 2 | 5  | 9.0  | 9.0  |
| -11 | 1 | 14 | 6.0  | 7.0  | -12 | 2 | 13 | 5.8  | 5.8  | -13 | 1 | 14 | 4.1  | 4.1  | 14 | 4 | 6  | 7.1  | 7.1  | 14 | 2 | 6  | 9.0  | 9.0  |
| -11 | 1 | 14 | 6.1  | 7.1  | -12 | 2 | 13 | 6.0  | 6.0  | -13 | 1 | 14 | 4.2  | 4.2  | 14 | 4 | 7  | 7.1  | 7.1  | 14 | 2 | 7  | 9.0  | 9.0  |
| -11 | 1 | 14 | 6.2  | 7.2  | -12 | 2 | 13 | 6.2  | 6.2  | -13 | 1 | 14 | 4.3  | 4.3  | 14 | 4 | 8  | 7.1  | 7.1  | 14 | 2 | 8  | 9.0  | 9.0  |
| -11 | 1 | 14 | 6.3  | 7.3  | -12 | 2 | 13 | 6.4  | 6.4  | -13 | 1 | 14 | 4.4  | 4.4  | 14 | 4 | 9  | 7.1  | 7.1  | 14 | 2 | 9  | 9.0  | 9.0  |
| -11 | 1 | 14 | 6.4  | 7.4  | -12 | 2 | 13 | 6.6  | 6.6  | -13 | 1 | 14 | 4.5  | 4.5  | 14 | 4 | 10 | 7.1  | 7.1  | 14 | 2 | 10 | 9.0  | 9.0  |
| -11 | 1 | 14 | 6.5  | 7.5  | -12 | 2 | 13 | 6.8  | 6.8  | -13 | 1 | 14 | 4.6  | 4.6  | 14 | 4 | 11 | 7.1  | 7.1  | 14 | 2 | 11 | 9.0  | 9.0  |
| -11 | 1 | 14 | 6.6  | 7.6  | -12 | 2 | 13 | 7.0  | 7.0  | -13 | 1 | 14 | 4.7  | 4.7  | 14 | 4 | 12 | 7.1  | 7.1  | 14 | 2 | 12 | 9.0  | 9.0  |
| -11 | 1 | 14 | 6.7  | 7.7  | -12 | 2 | 13 | 7.2  | 7.2  | -13 | 1 | 14 | 4.8  | 4.8  | 14 | 4 | 13 | 7.1  | 7.1  | 14 | 2 | 13 | 9.0  | 9.0  |
| -11 | 1 | 14 | 6.8  | 7.8  | -12 | 2 | 13 | 7.4  | 7.4  | -13 | 1 | 14 | 4.9  | 4.9  | 14 | 4 | 14 | 7.1  | 7.1  | 14 | 2 | 14 | 9.0  | 9.0  |
| -11 | 1 | 14 | 6.9  | 7.9  | -12 | 2 | 13 | 7.6  | 7.6  | -13 | 1 | 14 | 5.0  | 5.0  | 14 | 4 | 15 | 7.1  | 7.1  | 14 | 2 | 15 | 9.0  | 9.0  |
| -11 | 1 | 14 | 7.0  | 8.0  | -12 | 2 | 13 | 7.8  | 7.8  | -13 | 1 | 14 | 5.1  | 5.1  | 14 | 4 | 16 | 7.1  | 7.1  | 14 | 2 | 16 | 9.0  | 9.0  |
| -11 | 1 | 14 | 7.1  | 8.1  | -12 | 2 | 13 | 8.0  | 8.0  | -13 | 1 | 14 | 5.2  | 5.2  | 14 | 4 | 17 | 7.1  | 7.1  | 14 | 2 | 17 | 9.0  | 9.0  |
| -11 | 1 | 14 | 7.2  | 8.2  | -12 | 2 | 13 | 8.2  | 8.2  | -13 | 1 | 14 | 5.3  | 5.3  | 14 | 4 | 18 | 7.1  | 7.1  | 14 | 2 | 18 | 9.0  | 9.0  |
| -11 | 1 | 14 | 7.3  | 8.3  | -12 | 2 | 13 | 8.4  | 8.4  | -13 | 1 | 14 | 5.4  | 5.4  | 14 | 4 | 19 | 7.1  | 7.1  | 14 | 2 | 19 | 9.0  | 9.0  |
| -11 | 1 | 14 | 7.4  | 8.4  | -12 | 2 | 13 | 8.6  | 8.6  | -13 | 1 | 14 | 5.5  | 5.5  | 14 | 4 | 20 | 7.1  | 7.1  | 14 | 2 | 20 | 9.0  | 9.0  |
| -11 | 1 | 14 | 7.5  | 8.5  | -12 | 2 | 13 | 8.8  | 8.8  | -13 | 1 | 14 | 5.6  | 5.6  | 14 | 4 | 21 | 7.1  | 7.1  | 14 | 2 | 21 | 9.0  | 9.0  |
| -11 | 1 | 14 | 7.6  | 8.6  | -12 | 2 | 13 | 9.0  | 9.0  | -13 | 1 | 14 | 5.7  | 5.7  | 14 | 4 | 22 | 7.1  | 7.1  | 14 | 2 | 22 | 9.0  | 9.0  |
| -11 | 1 | 14 | 7.7  | 8.7  | -12 | 2 | 13 | 9.2  | 9.2  | -13 | 1 | 14 | 5.8  | 5.8  | 14 | 4 | 23 | 7.1  | 7.1  | 14 | 2 | 23 | 9.0  | 9.0  |
| -11 | 1 | 14 | 7.8  | 8.8  | -12 | 2 | 13 | 9.4  | 9.4  | -13 | 1 | 14 | 5.9  | 5.9  | 14 | 4 | 24 | 7.1  | 7.1  | 14 | 2 | 24 | 9.0  | 9.0  |
| -11 | 1 | 14 | 7.9  | 8.9  | -12 | 2 | 13 | 9.6  | 9.6  | -13 | 1 | 14 | 6.0  | 6.0  | 14 | 4 | 25 | 7.1  | 7.1  | 14 | 2 | 25 | 9.0  | 9.0  |
| -11 | 1 | 14 | 8.0  | 9.0  | -12 | 2 | 13 | 9.8  | 9.8  | -13 | 1 | 14 | 6.1  | 6.1  | 14 | 4 | 26 | 7.1  | 7.1  | 14 | 2 | 26 | 9.0  | 9.0  |
| -11 | 1 | 14 | 8.1  | 9.1  | -12 | 2 | 13 | 10.0 | 10.0 | -13 | 1 | 14 | 6.2  | 6.2  | 14 | 4 | 27 | 7.1  | 7.1  | 14 | 2 | 27 | 9.0  | 9.0  |
| -11 | 1 | 14 | 8.2  | 9.2  | -12 | 2 | 13 | 10.2 | 10.2 | -13 | 1 | 14 | 6.3  | 6.3  | 14 | 4 | 28 | 7.1  | 7.1  | 14 | 2 | 28 | 9.0  | 9.0  |
| -11 | 1 | 14 | 8.3  | 9.3  | -12 | 2 | 13 | 10.4 | 10.4 | -13 | 1 | 14 | 6.4  | 6.4  | 14 | 4 | 29 | 7.1  | 7.1  | 14 | 2 | 29 | 9.0  | 9.0  |
| -11 | 1 | 14 | 8.4  | 9.4  | -12 | 2 | 13 | 10.6 | 10.6 | -13 | 1 | 14 | 6.5  | 6.5  | 14 | 4 | 30 | 7.1  | 7.1  | 14 | 2 | 30 | 9.0  | 9.0  |
| -11 | 1 | 14 | 8.5  | 9.5  | -12 | 2 | 13 | 10.8 | 10.8 | -13 | 1 | 14 | 6.6  | 6.6  | 14 | 4 | 31 | 7.1  | 7.1  | 14 | 2 | 31 | 9.0  | 9.0  |
| -11 | 1 | 14 | 8.6  | 9.6  | -12 | 2 | 13 | 11.0 | 11.0 | -13 | 1 | 14 | 6.7  | 6.7  | 14 | 4 | 32 | 7.1  | 7.1  | 14 | 2 | 32 | 9.0  | 9.0  |
| -11 | 1 | 14 | 8.7  | 9.7  | -12 | 2 | 13 | 11.2 | 11.2 | -13 | 1 | 14 | 6.8  | 6.8  | 14 | 4 | 33 | 7.1  | 7.1  | 14 | 2 | 33 | 9.0  | 9.0  |
| -11 | 1 | 14 | 8.8  | 9.8  | -12 | 2 | 13 | 11.4 | 11.4 | -13 | 1 | 14 | 6.9  | 6.9  | 14 | 4 | 34 | 7.1  | 7.1  | 14 | 2 | 34 | 9.0  | 9.0  |
| -11 | 1 | 14 | 8.9  | 9.9  | -12 | 2 | 13 | 11.6 | 11.6 | -13 | 1 | 14 | 7.0  | 7.0  | 14 | 4 | 35 | 7.1  | 7.1  | 14 | 2 | 35 | 9.0  | 9.0  |
| -11 | 1 | 14 | 9.0  | 10.0 | -12 | 2 | 13 | 11.8 | 11.8 | -13 | 1 | 14 | 7.1  | 7.1  | 14 | 4 | 36 | 7.1  | 7.1  | 14 | 2 | 36 | 9.0  | 9.0  |
| -11 | 1 | 14 | 9.1  | 10.1 | -12 | 2 | 13 | 12.0 | 12.0 | -13 | 1 | 14 | 7.2  | 7.2  | 14 | 4 | 37 | 7.1  | 7.1  | 14 | 2 | 37 | 9.0  | 9.0  |
| -11 | 1 | 14 | 9.2  | 10.2 | -12 | 2 | 13 | 12.2 | 12.2 | -13 | 1 | 14 | 7.3  | 7.3  | 14 | 4 | 38 | 7.1  | 7.1  | 14 | 2 | 38 | 9.0  | 9.0  |
| -11 | 1 | 14 | 9.3  | 10.3 | -12 | 2 | 13 | 12.4 | 12.4 | -13 | 1 | 14 | 7.4  | 7.4  | 14 | 4 | 39 | 7.1  | 7.1  | 14 | 2 | 39 | 9.0  | 9.0  |
| -11 | 1 | 14 | 9.4  | 10.4 | -12 | 2 | 13 | 12.6 | 12.6 | -13 | 1 | 14 | 7.5  | 7.5  | 14 | 4 | 40 | 7.1  | 7.1  | 14 | 2 | 40 | 9.0  | 9.0  |
| -11 | 1 | 14 | 9.5  | 10.5 | -12 | 2 | 13 | 12.8 | 12.8 | -13 | 1 | 14 | 7.6  | 7.6  | 14 | 4 | 41 | 7.1  | 7.1  | 14 | 2 | 41 | 9.0  | 9.0  |
| -11 | 1 | 14 | 9.6  | 10.6 | -12 | 2 | 13 | 13.0 | 13.0 | -13 | 1 | 14 | 7.7  | 7.7  | 14 | 4 | 42 | 7.1  | 7.1  | 14 | 2 | 42 | 9.0  | 9.0  |
| -11 | 1 | 14 | 9.7  | 10.7 | -12 | 2 | 13 | 13.2 | 13.2 | -13 | 1 | 14 | 7.8  | 7.8  | 14 | 4 | 43 | 7.1  | 7.1  | 14 | 2 | 43 | 9.0  | 9.0  |
| -11 | 1 | 14 | 9.8  | 10.8 | -12 | 2 | 13 | 13.4 | 13.4 | -13 | 1 | 14 | 7.9  | 7.9  | 14 | 4 | 44 | 7.1  | 7.1  | 14 | 2 | 44 | 9.0  | 9.0  |
| -11 | 1 | 14 | 9.9  | 10.9 | -12 | 2 | 13 | 13.6 | 13.6 | -13 | 1 | 14 | 8.0  | 8.0  | 14 | 4 | 45 | 7.1  | 7.1  | 14 | 2 | 45 | 9.0  | 9.0  |
| -11 | 1 | 14 | 10.0 | 11.0 | -12 | 2 | 13 | 13.8 | 13.8 | -13 | 1 | 14 | 8.1  | 8.1  | 14 | 4 | 46 | 7.1  | 7.1  | 14 | 2 | 46 | 9.0  | 9.0  |
| -11 | 1 | 14 | 10.1 | 11.1 | -12 | 2 | 13 | 14.0 | 14.0 | -13 | 1 | 14 | 8.2  | 8.2  | 14 | 4 | 47 | 7.1  | 7.1  | 14 | 2 | 47 | 9.0  | 9.0  |
| -11 | 1 | 14 | 10.2 | 11.2 | -12 | 2 | 13 | 14.2 | 14.2 | -13 | 1 | 14 | 8.3  | 8.3  | 14 | 4 | 48 | 7.1  | 7.1  | 14 | 2 | 48 | 9.0  | 9.0  |
| -11 | 1 | 14 | 10.3 | 11.3 | -12 | 2 | 13 | 14.4 | 14.4 | -13 | 1 | 14 | 8.4  | 8.4  | 14 | 4 | 49 | 7.1  | 7.1  | 14 | 2 | 49 | 9.0  | 9.0  |
| -11 | 1 | 14 | 10.4 | 11.4 | -12 | 2 | 13 | 14.6 | 14.6 | -13 | 1 | 14 | 8.5  | 8.5  | 14 | 4 | 50 | 7.1  | 7.1  | 14 | 2 | 50 | 9.0  | 9.0  |
| -11 | 1 | 14 | 10.5 | 11.5 | -12 | 2 | 13 | 14.8 | 14.8 | -13 | 1 | 14 | 8.6  | 8.6  | 14 | 4 | 51 | 7.1  | 7.1  | 14 | 2 | 51 | 9.0  | 9.0  |
| -11 | 1 | 14 | 10.6 | 11.6 | -12 | 2 | 13 | 15.0 | 15.0 | -13 | 1 | 14 | 8.7  | 8.7  | 14 | 4 | 52 | 7.1  | 7.1  | 14 | 2 | 52 | 9.0  | 9.0  |
| -11 | 1 | 14 | 10.7 | 11.7 | -12 | 2 | 13 | 15.2 | 15.2 | -13 | 1 | 14 | 8.8  | 8.8  | 14 | 4 | 53 | 7.1  | 7.1  | 14 | 2 | 53 | 9.0  | 9.0  |
| -11 | 1 | 14 | 10.8 | 11.8 | -12 | 2 | 13 | 15.4 | 15.4 | -13 | 1 | 14 | 8.9  | 8.9  | 14 | 4 | 54 | 7.1  | 7.1  | 14 | 2 | 54 | 9.0  | 9.0  |
| -11 | 1 | 14 | 10.9 | 11.9 | -12 | 2 | 13 | 15.6 | 15.6 | -13 | 1 | 14 | 9.0  | 9.0  | 14 | 4 | 55 | 7.1  | 7.1  | 14 | 2 | 55 | 9.0  | 9.0  |
| -11 | 1 | 14 | 11.0 | 12.0 | -12 | 2 | 13 | 15.8 | 15.8 | -13 | 1 | 14 | 9.1  | 9.1  | 14 | 4 | 56 | 7.1  | 7.1  | 14 | 2 | 56 | 9.0  | 9.0  |
| -11 | 1 | 14 | 11.1 | 12.1 | -12 | 2 | 13 | 16.0 | 16.0 | -13 | 1 | 14 | 9.2  | 9.2  | 14 | 4 | 57 | 7.1  | 7.1  | 14 | 2 | 57 | 9.0  | 9.0  |
| -11 | 1 | 14 | 11.2 | 12.2 | -12 | 2 | 13 | 16.2 | 16.2 | -13 | 1 | 14 | 9.3  | 9.3  | 14 | 4 | 58 | 7.1  | 7.1  | 14 | 2 | 58 | 9.0  | 9.0  |
| -11 | 1 | 14 | 11.3 | 12.3 | -12 | 2 | 13 | 16.4 | 16.4 | -13 | 1 | 14 | 9.4  | 9.4  | 14 | 4 | 59 | 7.1  | 7.1  | 14 | 2 | 59 | 9.0  | 9.0  |
| -11 | 1 | 14 | 11.4 | 12.4 | -12 | 2 | 13 | 16.6 | 16.6 | -13 | 1 | 14 | 9.5  | 9.5  | 14 | 4 | 60 | 7.1  | 7.1  | 14 | 2 | 60 | 9.0  | 9.0  |
| -11 | 1 | 14 | 11.5 | 12.5 | -12 | 2 | 13 | 16.8 | 16.8 | -13 | 1 | 14 | 9.6  | 9.6  | 14 | 4 | 61 | 7.1  | 7.1  | 14 | 2 | 61 | 9.0  | 9.0  |
| -11 | 1 | 14 | 11.6 | 12.6 | -12 | 2 | 13 | 17.0 | 17.0 | -13 | 1 | 14 | 9.7  | 9.7  | 14 | 4 | 62 | 7.1  | 7.1  | 14 | 2 | 62 | 9.0  | 9.0  |
| -11 | 1 | 14 | 11.7 | 12.7 | -12 | 2 | 13 | 17.2 | 17.2 | -13 | 1 | 14 | 9.8  | 9.8  | 14 | 4 | 63 | 7.1  | 7.1  | 14 | 2 | 63 | 9.0  | 9.0  |
| -11 | 1 | 14 | 11.8 | 12.8 | -12 | 2 | 13 | 17.4 | 17.4 | -13 | 1 | 14 | 9.9  | 9.9  | 14 | 4 | 64 | 7.1  | 7.1  | 14 | 2 | 64 | 9.0  | 9.0  |
| -11 | 1 | 14 | 11.9 | 12.9 | -12 | 2 | 13 | 17.6 | 17.6 | -13 | 1 | 14 | 10.0 | 10.0 |    |   |    |      |      |    |   |    |      |      |

Table 2 (cont.)

|       |       |        |       |
|-------|-------|--------|-------|
| H(3)  | 0.331 | -0.043 | 0.051 |
| H(4)  | 0.380 | 0.215  | 0.130 |
| H(5)  | 0.418 | 0.457  | 0.226 |
| H(6)  | 0.401 | 0.604  | 0.178 |
| H(7)  | 0.358 | 0.609  | 0.251 |
| H(8)  | 0.200 | 0.620  | 0.200 |
| H(9)  | 0.066 | 0.620  | 0.144 |
| H(10) | 0.024 | 0.459  | 0.104 |
| H(11) | 0.026 | 0.443  | 0.181 |
| H(12) | 0.040 | -0.098 | 0.040 |

The final structure factors, including the contribution of the hydrogen atoms, reduced  $R$  to 0.122 for all observed reflexions and to 0.155 for all reflexions.

### Description of the structure

Final structure parameters and standard deviations are given in Table 3. Bond lengths and bond angles are shown in Fig. 2, and in Table 4, together with their standard deviations.

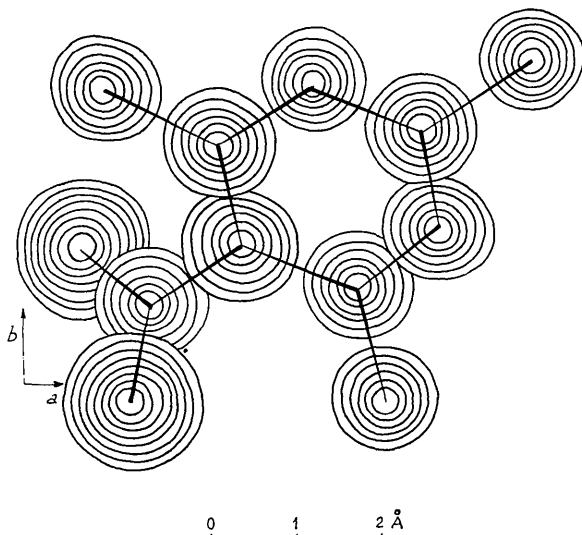


Fig. 1. 2,4,6-Trimethylbenzoic acid. A composite diagram of the final electron density function; the contours are drawn at equal intervals of  $1.5 \text{ e.}\text{\AA}^{-3}$ , starting from  $1.5 \text{ e.}\text{\AA}^{-3}$ .

Table 4. Bond lengths and valence angles with e.s.d. in parentheses

|            |                    |                |                 |
|------------|--------------------|----------------|-----------------|
| C(1)-C(2)  | 1.382 Å<br>(0.006) | C(1)-C(2)-C(3) | 120.1°<br>(0.4) |
| C(2)-C(3)  | 1.398<br>(0.006)   | C(2)-C(3)-C(4) | 120.1<br>(0.4)  |
| C(3)-C(4)  | 1.390<br>(0.006)   | C(3)-C(4)-C(5) | 119.2<br>(0.4)  |
| C(4)-C(5)  | 1.380<br>(0.006)   | C(4)-C(5)-C(6) | 121.7<br>(0.4)  |
| C(5)-C(6)  | 1.402<br>(0.006)   | C(5)-C(6)-C(1) | 118.3<br>(0.4)  |
| C(6)-C(1)  | 1.395<br>(0.006)   | C(6)-C(1)-C(2) | 120.6<br>(0.4)  |
| C(1)-C(7)  | 1.491<br>(0.006)   | C(6)-C(1)-C(7) | 118.4<br>(0.4)  |
| C(2)-C(8)  | 1.547<br>(0.007)   | C(2)-C(1)-C(7) | 121.0<br>(0.4)  |
| C(4)-C(9)  | 1.533<br>(0.009)   | C(1)-C(2)-C(8) | 123.3<br>(0.4)  |
| C(6)-C(10) | 1.538<br>(0.007)   | C(3)-C(2)-C(8) | 116.6<br>(0.4)  |
| C(7)-O(1)  | 1.250<br>(0.006)   | C(3)-C(4)-C(9) | 119.9<br>(0.5)  |
| C(7)-O(2)  | 1.286<br>(0.006)   | C(5)-C(4)-C(9) | 120.9<br>(0.5)  |

Table 3. Atomic parameters for the non-hydrogen atoms

E.s.d.'s are in parentheses.

|       | $x/a$              | $y/b$               | $z/c$              | $B_{11}^*$ | $B_{22}$ | $B_{33}$ | $B_{12}$ | $B_{23}$ | $B_{31}$ |
|-------|--------------------|---------------------|--------------------|------------|----------|----------|----------|----------|----------|
| C(1)  | 0.1648<br>(0.0003) | 0.2257<br>(0.0006)  | 0.0990<br>(0.0002) | 4.52       | 2.77     | 2.73     | -0.39    | 0.28     | 0.35     |
| C(2)  | 0.2500<br>(0.0003) | 0.1512<br>(0.0006)  | 0.0938<br>(0.0002) | 4.67       | 2.94     | 3.35     | 0.16     | -0.23    | -0.03    |
| C(3)  | 0.3185<br>(0.0003) | 0.2483<br>(0.0007)  | 0.1331<br>(0.0002) | 5.43       | 4.80     | 4.62     | -0.06    | -0.01    | 0.15     |
| C(4)  | 0.3031<br>(0.0004) | 0.4149<br>(0.0007)  | 0.1710<br>(0.0002) | 5.26       | 4.40     | 3.33     | -1.16    | -0.35    | -0.20    |
| C(5)  | 0.2186<br>(0.0003) | 0.4896<br>(0.0006)  | 0.1733<br>(0.0002) | 5.36       | 3.32     | 3.23     | -0.64    | -0.60    | 0.76     |
| C(6)  | 0.1482<br>(0.0003) | 0.3982<br>(0.0006)  | 0.1371<br>(0.0002) | 4.86       | 2.87     | 3.67     | 0.00     | 0.21     | 0.95     |
| C(7)  | 0.0907<br>(0.0003) | 0.1296<br>(0.0006)  | 0.0583<br>(0.0002) | 3.82       | 2.82     | 3.60     | -0.68    | 0.34     | -0.22    |
| C(8)  | 0.2725<br>(0.0004) | -0.0353<br>(0.0007) | 0.0555<br>(0.0003) | 7.55       | 3.09     | 5.64     | 0.82     | -0.82    | 0.00     |
| C(9)  | 0.3797<br>(0.0005) | 0.5259<br>(0.0012)  | 0.2089<br>(0.0004) | 6.88       | 8.76     | 7.66     | -2.23    | -2.65    | -1.55    |
| C(10) | 0.0566<br>(0.0004) | 0.4870<br>(0.0008)  | 0.1435<br>(0.0004) | 7.08       | 5.74     | 8.17     | 0.66     | -0.30    | 0.59     |
| O(1)  | 0.0404<br>(0.0003) | 0.2205<br>(0.0006)  | 0.0147<br>(0.0002) | 5.61       | 4.04     | 7.09     | -0.84    | 0.79     | -1.91    |
| O(2)  | 0.0823<br>(0.0003) | -0.0502<br>(0.0006) | 0.0692<br>(0.0003) | 8.34       | 3.65     | 7.90     | -1.94    | 1.22     | -2.84    |

\* In the expression  $F_o \exp[-\frac{1}{4}(B_{11}h^2a^{*2} + \dots + B_{13}2hla^*c^*)]$ .

Table 4 (cont.)

|                 |                 |
|-----------------|-----------------|
| C(5)-C(6)-C(10) | 117.50<br>(0.4) |
| C(1)-C(6)-C(10) | 124.2<br>(0.4)  |
| C(1)-C(7)-O(1)  | 121.0<br>(0.4)  |
| C(1)-C(7)-O(2)  | 116.7<br>(0.4)  |
| O(1)-C(7)-O(2)  | 122.2<br>(0.4)  |

Bond distances and angles in the benzene ring are normal (mean values 1.391 Å and 120°). The exocyclic C(2)-C(8), C(6)-C(10) and C(4)-C(9) bond lengths are 1.547, 1.538 and 1.533 Å respectively, also in good agreement with the value of 1.53 Å given for this type of bond.

The distance C(1)-C(7) of 1.491 Å is a little larger than the value of 1.479 Å reported for the  $sp^2$  hybridization state. The same observation has been made in *o*-chlorobenzoic acid (Ferguson & Sim, 1961) and in 2,6-dimethylbenzoic acid (Anca *et al.*, 1967); in these acids the corresponding values are 1.521 and 1.525 Å respectively. This increase in bond length is a result of molecular overcrowding, and the fact that in the compound 2,4,6-trimethylbenzoic acid the corresponding increase is rather smaller may be due to the presence of the third methyl group in the *para* position.

The C(7)-O(1) bond of 1.250 Å is noticeably shorter than the C(7)-O(2) bond of 1.286 Å showing that the hydrogen atom is attached to O(2). That is also in good agreement with the value of the angle C(1)-C(7)-O(2) (116.7°), which is smaller than the angle C(1)-C(7)-O(1) (121.0°).

The equation of the least-squares plane through the carbon atoms of the benzene ring calculated according to Schomaker, Waser, March & Bergman (1959) with unit weight for all atoms is:

$$0.1794X' + 0.5094Y - 0.8416Z' - 0.2114 = 0,$$

where  $X'YZ'$  (in Å), are referred to the orthogonal axes  $a$ ,  $b$  and  $c'$ . The deviations in Å of the individual atoms from the plane are shown in column (ii) of Table 5.

Table 5. Displacements (Å)  
of the atoms from the various planes

- (i) Plane through all atoms  
(ii) Plane through benzene  
(iii) Plane through atoms C(1), C(7), O(1), O(2)

|       | (i)    | (ii)   | (iii)  |
|-------|--------|--------|--------|
| C(1)  | -0.017 | 0.005  | -0.002 |
| C(2)  | 0.041  | -0.007 | -0.902 |
| C(3)  | 0.061  | 0.001  | -0.935 |
| C(4)  | 0.008  | 0.007  | -0.052 |
| C(5)  | -0.079 | -0.010 | 0.860  |
| C(6)  | -0.080 | 0.003  | 0.897  |
| C(7)  | 0.024  | 0.061  | 0.003  |
| C(8)  | 0.126  | 0.008  | -1.934 |
| C(9)  | 0.049  | 0.036  | -0.105 |
| C(10) | -0.181 | -0.017 | 1.954  |
| O(1)  | 0.814  | 0.895  | -0.003 |
| O(2)  | -0.766 | -0.767 | -0.003 |

The least-squares plane through all atoms in the molecule is:

$$0.2201X' + 0.4740Y - 0.8526Z' - 0.1630 = 0,$$

and the plane through the carboxyl group and C(1) of the benzene ring is:

$$-0.6104X' + 0.1859Y + 0.7700Z' + 0.1142 = 0.$$

The atoms C(8), C(9) and C(10), Table 5, show deviations above and below the best ring-plane which are larger than the deviations of the carbon atoms of the benzene ring. This fact is probably due to an overcrowded molecular structure. This molecular overcrowding is better manifested by the rotation of the carboxylic group about the exocyclic bond C(1)-C(7), the dihedral angle between the mean plane of the benzene ring and the mean plane of C(1), C(7), O(1) and O(2) being 48°29'.

The value found here, which is greater than that for other benzoic acids, is, however, smaller than the corresponding tilt of 53°31', found by Anca *et al.* (1967) for 2,6-dimethylbenzoic acid. Such a decrease may be due to the presence of the methyl group in the *para* position.

There is a mutual interaction between the COOH group and the two CH<sub>3</sub> groups in *ortho* positions, resulting in a slight opening of the valence angles C(1)-C(6)-C(10) and C(1)-C(2)-C(8), which have values of 124.2 and 123.3°, and a corresponding shortening of the valence angles C(10)-C(6)-C(5) and C(8)-C(2)-C(3) which have values of 117.5 and 116.6°; all these angles differ from the normal value of 120°.

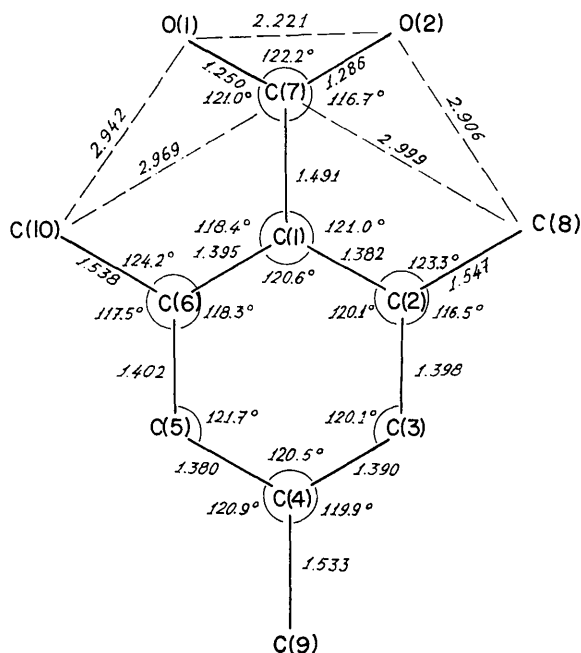


Fig. 2. Bond lengths and angles in the 2,4,6-trimethylbenzoic acid molecule.



Table 6. *Intermolecular distances less than 4 Å*

The following Roman numbers give the symmetry relationship of the atoms concerned

|  | I   | x               | y                | z               | VI   | $\frac{1}{2}+x$ | $\frac{1}{2}+y$  | z               |
|--|-----|-----------------|------------------|-----------------|------|-----------------|------------------|-----------------|
|  | II  | $\frac{1}{2}-x$ | $\frac{1}{2}-y$  | -z              | VII  | $\frac{1}{2}-x$ | $\frac{1}{2}+y$  | $\frac{1}{2}-z$ |
|  | III | $\frac{1}{2}-x$ | $-\frac{1}{2}+y$ | $\frac{1}{2}-z$ | VIII | -x              | 1-y              | -z              |
|  | IV  | -x              | -y               | -z              | IX   | x               | 1+y              | z               |
|  | V   | 1-x             | y                | $\frac{1}{2}-z$ | X    | $\frac{1}{2}-x$ | $-\frac{1}{2}-y$ | -x              |

|      | i | j    | d(ij) |         | i     | j | d(ij) |      |         |
|------|---|------|-------|---------|-------|---|-------|------|---------|
| C(1) | I | C(2) | II    | 3.796 Å | C(7)  | I | O(1)  | IV   | 3.407 Å |
| C(1) | I | C(8) | II    | 3.607   | C(7)  | I | O(2)  | IV   | 3.477   |
| C(1) | I | C(9) | III   | 3.721   | C(8)  | I | C(8)  | X    | 3.649   |
| C(2) | I | C(2) | II    | 3.684   | C(8)  | I | O(1)  | II   | 3.816   |
| C(2) | I | C(7) | II    | 3.989   | C(9)  | I | C(9)  | V    | 3.910   |
| C(2) | I | C(8) | II    | 3.811   | C(9)  | I | O(2)  | VI   | 3.998   |
| C(2) | I | O(1) | II    | 3.881   | C(9)  | I | O(2)  | VII  | 3.963   |
| C(3) | I | C(5) | III   | 3.898   | C(10) | I | O(1)  | VIII | 3.740   |
| C(3) | I | C(7) | II    | 3.742   | C(10) | I | O(2)  | IX   | 3.523   |
| C(3) | I | O(1) | II    | 3.388   | O(1)  | I | O(1)  | IV   | 3.372   |
| C(6) | I | C(8) | II    | 3.731   | O(1)  | I | O(2)  | IV   | 2.648*  |
| C(6) | I | C(9) | III   | 3.776   | O(2)  | I | O(2)  | IV   | 3.538   |
| C(7) | I | C(7) | IV    | 3.869   |       |   |       |      |         |

\* Hydrogen bond.

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## Structural Changes in the Alloy Systems of Mg-Zn-Cu and Mg-Zn-Ag Related to the Friauf-Laves Phases

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In the pseudo-binary alloy systems of MgZn<sub>2</sub>-MgCu<sub>2</sub> and MgZn<sub>2</sub>-MgAg<sub>2</sub> three new stacking variants were found in the homogeneity ranges of the C<sub>14</sub> and C<sub>36</sub> structures. These three structures can be expressed, in terms of the stacking sequence of six compound layers, as 8-layer (AB'AB'A'CA'C), 9-layer (AB'ABC'BCA'C) and 10-layer (ABC'BCA'C'BC'B') type. Representation of the Friauf-Laves phases and of relevant layer structures is discussed in connexion with that of the closest packing of spheres.

Among several factors governing the crystal structures of alloy phases or intermetallic compounds, the electron concentration is important in relation to the interaction between the Fermi surface and Brillouin-zone boundaries. Laves & Witte (1936) investigated alloys of Mg-base ternary Friauf-Laves phases\* and found that,

when, for instance, Cu in MgCu<sub>2</sub> is replaced by a metal of higher valency, such as Zn, Al or Si, the cubic C<sub>15</sub> (MgCu<sub>2</sub>) structure is followed by the C<sub>36</sub> (MgNi<sub>2</sub>) and C<sub>14</sub> (MgZn<sub>2</sub>) structures as the electron-atom ratio (*e/a*) is increased. This work indicated a close relationship between electron concentration and crystal structure, because the phase boundaries for the above three types of structure appeared at almost the same electron concentration for various combinations of metals.

\* The term 'Friauf-Laves phases' is used in this paper for the C<sub>14</sub>, C<sub>15</sub> and C<sub>36</sub> type structures, since there has been confusion in specifying these types of phase. The structures of MgCu<sub>2</sub> and MgZn<sub>2</sub> were originally determined by Friauf (1927*a, b*) and that of MgNi<sub>2</sub> by Laves & Witte (1935). New stacking variants reported in this paper are classified in terms of structures related to Friauf-Laves phases. (We are grateful for Dr S. Samson's suggestion on this point.)

We re-investigated the pseudo-binary systems of MgZn<sub>2</sub>-MgCu<sub>2</sub>, MgZn<sub>2</sub>-MgAg<sub>2</sub>, MgCu<sub>2</sub>-MgAl<sub>2</sub>, MgCu<sub>2</sub>-MgSi<sub>2</sub> and MgCu<sub>2</sub>-MgNi<sub>2</sub>, and confirmed that the crystal structures of the systems Mg-Zn-Cu and Mg-Zn-Ag were strongly governed by the electron